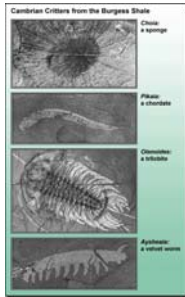


## Computational Development



- Life on earth was single-celled for 3 billion years
- Multicellular life appeared at the Cambrian Explosion,
- Large organisms with many body plans appeared
- Exploited new niches

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## Computational Development (2)

- EC is limited to small problems like acellular life
- A Cambrian Explosion in EC might allow the evolution of solutions to large and complex problems
  - Microprocessor design
  - Passenger jet design
  - Skyscraper design
- The process that turns a single cell into a large organism is *development*

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## Benefits of Development

- Primarily *scalability*:
- Evolution creates large, complex phenotypes using development
- It's the only solution nature found in 4 billion years
- By modelling features of development we might be able to create large complex phenotypes too

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## Other Benefits

- Multicellular organisms are fault tolerant
  - Redundancy on many levels
- The developmental process itself is robust to faults
  - Splitting an embryo produces twins
  - Starfish, newts regrow missing limbs
  - These phenomena rely on development
- So developmental robustness provides another avenue to fault tolerance
- Biological development is poorly understood
  - Modelling might provide insight into how it really works

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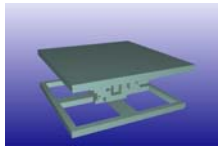
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## Other Benefits (2)

- 2D / 3D structure design
  - nature has evolved a way to map from 1D chromosomes to 3D structures over aeons
  - the basic concepts might allow us to easily map to 2D structures too



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## Problems that might benefit from scalability

- Problems where we know that EC is outperformed by other methods are currently under exploration:
  - Circuit design (c.f. traditional methodologies)
  - Software design (c.f. traditional methodologies)
  - ANN design (c.f. biological NN design)
- But in reality many problems are eventually limited by the scalability of EAs

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## What is the scalability problem?

- EC works well with small chromosomes
  - Small search space, easily sampled
- Large chromosomes don't work well
  - Combinatorial explosion of search space
  - EC can't sample space effectively
  - Converges to suboptimal solution
- Why?

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## Relating Schema Theorem

- We can think of it in terms of schema theorem
- Large, high order schemata are likely to be disrupted by evolutionary operators
- Solutions to large real-world problems are likely require large, high order schemata

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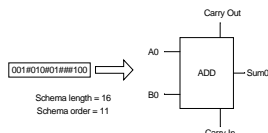
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## Toy Example: Adders



- A 1 bit adder can be evolved easily
- Assume fitness is only rewarded when perfect schema is discovered
- (In reality fitness reward is more gradual)
- Evolution must discover length 16, order 11 schema before fitness reward

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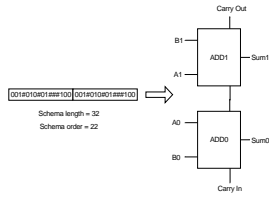
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## Toy Example: Adders (2)



- A 2 bit adder can be made by joining 2x1 bit adder
- Evolution must learn the design for ADD 1 independently of its discovery of ADD0
- A pain, but not a show-stopper

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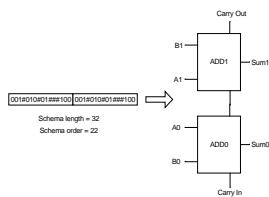
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## Epistasis



- The problem is worse:
- Output Sum1 *relies on* the carry out from ADD0
- ∴ Fitness from Sum1 will only be rewarded if ADD0 is intact
- Fitness for ADD1 only rewarded if requires schema twice as long and twice as big as the schema for Sum0
- Linkage between genes that results in nonlinear fitness payoff is called *epistasis*

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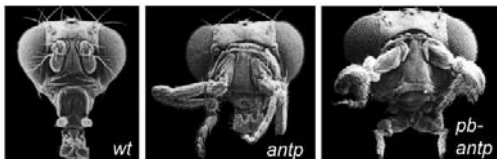
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## How does development tackle large problems

- We don't completely know, but:
- A mutation in a single gene can transform one complex feature into another
- e.g. antennae->legs, proboscis->legs




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### What does this mean?

- One gene can't describe an entire leg design
- Nature seems to have a simple mechanism to *reuse* leg design
- The generation of the mis-placed legs is almost perfect
- As they develop they are not *interacting* with the surrounding tissues
- Its generation seems to be *independent* of surrounding tissues
- It can be thought of as a developmental *module*.

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### How can this improve adder evolution?

- Large adders could be built by *re-using* the 1 bit adder design
- A bias towards *modules* that do not interact might minimise the problem of epistasis
- Later it will be shown how development allows re-use and provides modularity
- Later it will be shown how we can model development to gain these features

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### Fundamental Processes – Regional Specification

- RS is simply pattern formation
- Process where spatial and temporal pattern of cell activities is organised
- Cells acquire different identities
- Identities defined by chemical differences
- Differentiation into functional cell types happens later
- Occurs throughout early stages of development

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### Fundamental Processes – Cell Differentiation

- Cells become structurally and functionally different from each other
- Cells assume one of a few distinct cell types
  - e.g. skin, liver etc
- One-way process
- Gradual process, occurs throughout development

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### Fundamental Processes - Morphogenesis

- Movement of cells and tissues that alter the form of the embryo
- Active during early/mid-development
- Many strategies
  - Alteration in cell adhesion
  - Cell division
  - Apoptosis (Programmed cell death)

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### Fundamental Processes - Growth

- Embryos do not increase in size until the basic structure of the embryo has developed
- Most size increase results from growth at the end of development
- Growth is mostly due to cell division
- Some morphogenesis can arise through differences in growth rates of cells

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## Differential Gene Activation

- Development's engine is gene activation, producing proteins
- Engine is directed by the differential activation of genes
- Activation of genes in different cells produces different chemical environments
- Gives cells different identities, allows differentiation
- The majority of DGA results from DNA *transcription*

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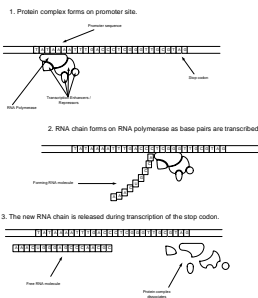
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## DNA Transcription



- Protein complex binds to a gene
- Complex travels along gene
- Generates complementary RNA
- RNA translated into protein by cellular machinery
- Complex made of proteins called *transcription factors*
- Complex is gene-specific
- Correct combination of TFs must be present for gene to be transcribed
- ∴ TFs control transcription rate
- Transcription factors are themselves gene products

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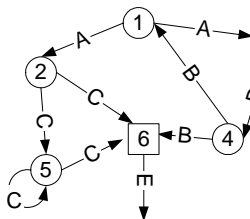
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## Gene Regulatory Networks



- Gene interaction can be modelled as a network
- GRN is a directed graph with labelled nodes and edges
- Nodes represent genes
- Edges represent gene products (TFs)
- Edges link parent to regulated gene
- Genes generate a single TF
- TFs can control multiple genes

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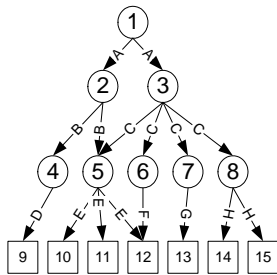
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## GRNs Capture Modularity



- GRNs capture one possible mechanism for modularity
- Activation of a single master control gene causes a cascade of gene activity
- This can generate a complex feature in the phenotype
- The genes involved are a developmental *module*

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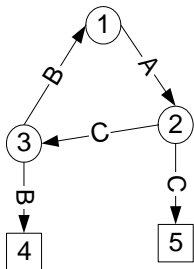
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## GRNs Capture Re-use



- GRNs capture one possible mechanism for re-use
- A feedback loop in a GRN can cause a gene to be activated multiple times
- If it is a master control gene it may allow re-use of a complex feature

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## Intercellular Communication

- DGA explains how cells can differentiate
- DGA explains how a gene can be repeatedly activated
- Doesn't explain how development forms iterative structures over space
  - segments
- This requires information to be transferred between cells
- 2 mechanisms
  - Cell division
  - Cell induction

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## Communication – Cell Division

- Cell division occurs twice
  - embryo cleavage
  - growth
- *Cytoplasmic determinant*: substance that guarantees that a cell assumes a particular state
- Inhomogeneities occur in CD concentrations within cells
- Cells divide
- Daughter cells contain different concentrations
- Results in cells with different states

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## Communication - Induction

- The main form of intercellular communication
- Transmission of chemical signals b/w cells
- Proteins (gene products) too big to pass through cell membranes
- Nature must use more complex processes

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## Methods of Induction

1. Intercellular proteins bind to receptors in cell membrane
  - activates a TF in the cell
2. Protein catalyses production of small molecule
  - passes through both cell membranes
3. TFs interact directly before cleavage
  - no cell membranes present
4. Pass signal through gap junction
  - cells must be touching

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## Models of Development used in EC

- Anything that the genotype is *executed* as a program to generate the phenotype
  - i.e. the phenotype 'grows'
- Models of development are surprisingly common
  - e.g. a tree can describe growth rules
  - it could be evolved using GP
- This is a very broad description – most models have more in common with biological development
- Developmental models can be broken into
  - Explicit
  - Implicit
    - L-Systems
    - Cellular

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## Explicit Development

- Developmental program is applied to a fixed 'embryonic' phenotype
- Explicitly specifies each developmental step like a computer program
- GP often used to represent the developmental program
- Nodes contain growth & modification instructions
  - Split component, change component,

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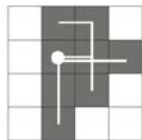
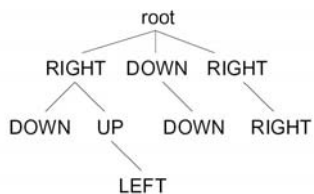
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## Explicit Development: Toy Example



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## Where's the benefit?

- No implicit modularity
- No implicit re-use

BUT

- Additional control structures can provide this:
  - Modularity (e.g. ADFs)
  - Iteration (e.g. ADIs, ADLs)
  - Recursion (e.g. ADRs)

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## Implicit Development

- Similar to the GRN model used in biology
- Consists of a set of rules
- Rule set implicitly defines a program through their interactions
- Rule's postcondition can be thought of as modelling a gene product
- Rule precondition can be thought of as modelling transcription factors required for rule activation
- Current work generally decomposes into 2 approaches:
  - L-Systems
  - Cellular

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## L-Systems

- An L-System is a set of rules
- Applied to a string called an *axiom*
- If symbol in rule's precondition is found in string it is replaced with symbols in rule's postcondition
- Successive applications repeatedly rewrite the string
  
- Rules are applied in parallel
  
- In most L-Systems:
  - Rule precondition is always only one symbol long
  - Rule postcondition is one or more symbols

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## L-System Example

- Can generate a long string from a short one
- Rules are encoded in a chromosome
- Axiom is pre-defined
- During evaluation string is rewritten until stopping conditions met
- Final string is then usually interpreted as a series of growth instructions to generate phenotype
- Allows small chromosome to generate arbitrarily large phenotype

A	→	BC	A
<b>B</b>	→	EF	BC
C	→	G	EFG

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## How Is It Like Development?

- Axiom is like an embryo
- Rules are like genes
- Rule postconditions are a bit like gene products
- Rule preconditions are a bit like transcription factors
- Does not model biological development particularly closely
- Developed to model growth in plants

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## What's the benefit?

A → BC  
**B** → EF  
 C → GHI

A  
 BC  
 EFGHI

A → BC  
**B** → AD  
 C → C  
 D → D

A  
 BC  
 ADC  
 BCDC  
 ADCDC  
 BCDCDC

- L-Systems capture modularity
- L-Systems capture re-use
- Gene products interpreted as a program
- Great success modelling plants

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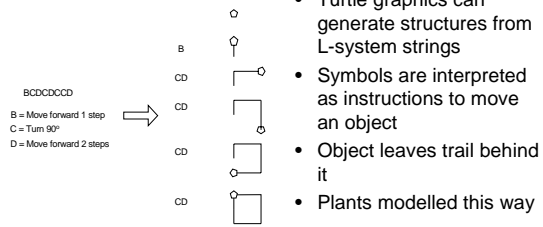
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## Turtle Graphics




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## Disadvantages

- Doesn't inherently map to sensible 2D/3D operations
  - Can be interpreted as *instructions*: growth, turtle etc.
  - If you want 2D/3D structure then other approaches might be more suitable
- The bigger problem is that they are *context-free*

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## Context-Free vs. Context Sensitive

- Context-free rules have only one symbol in their precondition
- All instances of the symbol found in the string are re-written
- Context-sensitive rules have more than one symbol in their precondition
- Only substrings that match the rule are rewritten
- This means that a symbol's neighbours affect what happens to it
- i.e. the *context* that the symbols are found in alters the developmental process

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## Benefits of Context

- How can context be useful?
  - Context allows more precise control over how development proceeds
  - Might be useful to use environmental cues as context
    - plants grow towards light
    - neurons are guided by chemical gradients

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## Cellular Models

- Similar to production rules
- Usually designed to model biology more closely
  - Use terms like genes, proteins etc. to describe rules
- Context sensitive rules
- Product of rule interaction is phenotype
  - not instructions to build it, c.f. L-Systems
- Effectively 2D or 3D context sensitive production rules

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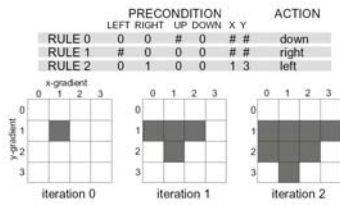
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## Cellular: Toy Example



- Rules applied to every filled cell
- Cells are sensitive to left, right, above, below neighbours
- In precondition 0: Absent, 1: Present, # Don't care
- Cells are sensitive to concentration of 2 chemicals, X and Y
- Rule only fires if 4 terms in precondition are true
- Rules applied in parallel

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## Cellular Features

- Cellular systems model Biology a lot more closely
- Rules interact and can be modelled with GRNs
- Context-sensitivity is communication between cells
- Development works by producing increasingly large and complex patterns of proteins from simple starting conditions
- Communication between cells can allow re-use over space: see following e.g.

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## Cellular – Adder Example

- 2 D array of cells
- 2 layers to each cell: Protein layer & Architecture layer
- Development carried out for 30 timesteps
- 2 Types of rules
  - Regulatory: Affect how proteins interact in the protein layer
  - Architecture: Affect how the circuit develops over time

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## Protein Layer

- Only concerned with how proteins interact
- Each cell communicates with 4 neighbours
- 4 proteins (A,B,C,D) interact through a set of rules
- Cells generate proteins in unit concentrations
- Rule precondition specifies what proteins must be present or absent for rule activation
- Rule postcondition defines what protein is generated
- Must set simple starting conditions somewhere in the array to begin protein generation

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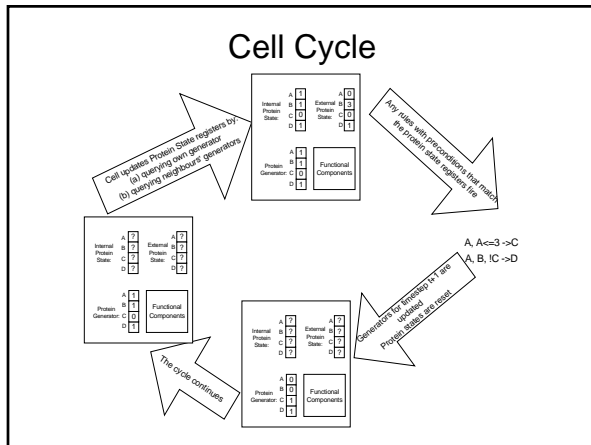
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## Cell Cycle




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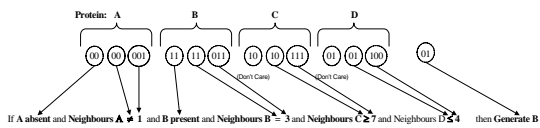
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## Rule Structure



- For each protein: 2 terms in precondition
- 1<sup>st</sup> term, tests cell's internal protein conc.: T,F,D/C
- 2<sup>nd</sup> term tests external protein conc.
- 1<sup>st</sup> 2 bits: precedence or inequality operator: !=, <=, >=, ==
- Final 3 bit: Concentration value: Value b/w 0 & 7
- Concentration values >4 can be used as don't cares, don't fires
- If all 8 terms are true, rule fires and protein is generated
- Postcondition defines which protein is generated

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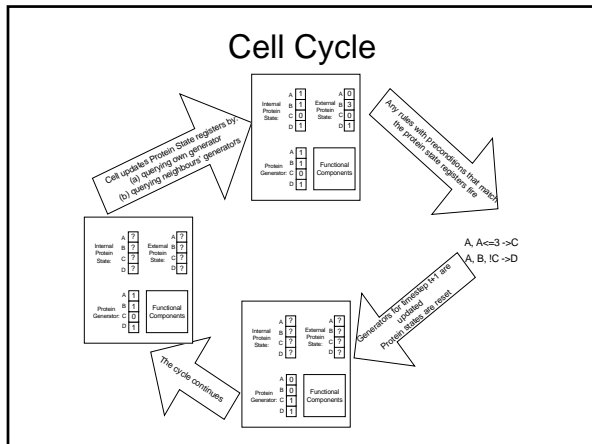
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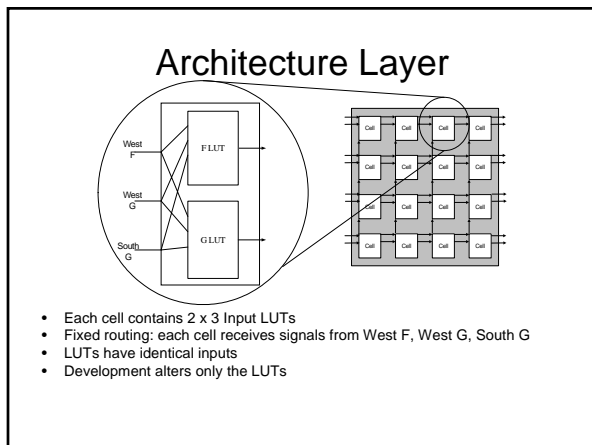
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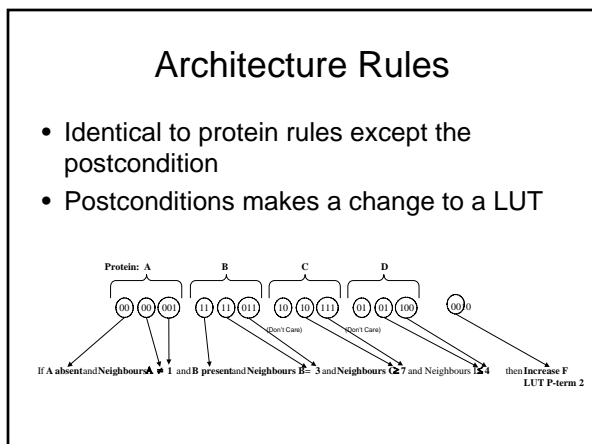
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## Architecture Postconditions

Postcond.	Action
0000	Increase F LUT P-term 0 Counter
0001	Increase F LUT P-term 1 Counter
0010	Increase F LUT P-term 2 Counter
0011	Increase F LUT P-term 3 Counter
0100	Increase F LUT P-term 4 Counter
0101	Increase F LUT P-term 5 Counter
0110	Increase F LUT P-term 6 Counter
0111	Increase F LUT P-term 7 Counter
1000	Increase G LUT P-term 0 Counter
1001	Increase G LUT P-term 1 Counter
1010	Increase G LUT P-term 2 Counter
1011	Increase G LUT P-term 3 Counter
1100	Increase G LUT P-term 4 Counter
1101	Increase G LUT P-term 5 Counter
1110	Increase G LUT P-term 6 Counter
1111	Increase G LUT P-term 7 Counter

- Each cell also contains a set of *counters*
- There is 1 counter for each LUT Entry
- When an architecture rule fires it increments a counter

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## Mapping to a Circuit

- At the end of development each of the cell counters is queried
- If the counter value  $\geq$  a pre-defined threshold the LUT entry is set TRUE
- Otherwise the LUT entry is set FALSE
- Architecture rules fire at different rates in different cells
- Models gradual differentiation found in biological development
- $\therefore$  LUT entries set/not set in different cells
- Evolution used to find rule set that set LUTs to form adder

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## Evolving Rules

- Chromosome: 20 protein rules + 14 arch rules  
 $\therefore$  Length = 1048 bits
- Population 100
- Random Initialisation
- Tournament Selection 80%
- Uniform Crossover 75%
- Point Mutation: 5 Muts. per chrom.
- Generations: 2500 or optimal solution

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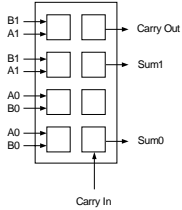
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## Example: 2 Bit Adder With Carry



- Task is to evolve a 2 Bit adder *with carry*
- 5 inputs, 3 outputs
- 2x4 array of FPGA cells developed
- Set starting conditions to Cell 0: A=1, Cell 4: B=1
- Inputs and output points as shown
- Pass all possible input combinations one at a time
- Measure total number of output bits correct for each input combination
- Fitness = sum(correct output bits) MAX 96

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## Evolved Rules

Protein Rules:

- 1 A==7,B,B==2,C,C!=1,!D,D==0,->D
- 2 A>=7,B!=0,C==6,!D,D>=4,->A
- 3 !A,A<=4,!B,B>=4,!C,C<=4,D,D<=4,->D
- 4 !A,A<=2,B<=0,C,C!=6,D!=5,->B
- 5 A,A>=5,B,B>=3,C!=6,D==0,->C
- 6 !A,A<=4,!B,B!=4,C>=1,D<=0,->D
- 7 A>=2,B,B!=7,!C,C>=4,D==3,->A
- 8 A<=1,B,B>=1,C,C==7,!D,D<=4,->C
- 9 A==4,B,B!=0,C!=5,D>=0,->C
- 10 !A,A!=3,B!=1,!C,C<=7,D!=0,->C
- 11 A==6,B==0,C>=1,!D,D!=1,->D
- 12 A>=3,B==4,C==4,D==2,->A
- 13 A==0,B,B!=7,C!=1,D!=1,->C
- 14 A,A<=2,!B,B>=3,C!=5,D,D!=0,->C
- 15 A,A>=7,B,B<=6,C,C<=4,D>=2,->D
- 16 !A,A<=4,B>=3,C==5,D>=6,->A
- 17 A!=0,B,B>=6,C,C<=3,D<=4,->A
- 18 A,A<=2,B<=4,C,C>=2,D!=4,->B
- 19 A>=7,!B,B==1,!C,C<=2,!D,D>=1,->D
- 20 A!=6,!B,B>=5,C>=0,!D,D!=7,->A

Architecture rules:

- 1 A<=2,B,B==1,C>=5,!D,D!=0,G: 5
- 2 A>=3,!B,B>=5,C<=2,D!=5,F: 0
- 3 A!=1,B<=5,C<=3,!D,D>=0,F: 7
- 4 !A,A<=6,B!=4,C!=1,D<=5,G: 1
- 5 A!=3,B>=4,!C,C>=1,D,D!=3,G: 4
- 6 A==0,B!=6,!C,C!=7,D<=7,F: 0
- 7 A,A!=6,!B,B<=5,C,C<=7,D<=4,G: 0
- 8 !A,A<=4,!B,B!=3,C!=4,!D,D<=5,G: 7
- 9 A==0,B<=3,C,C<=1,D==0,F: 3
- 10 !A,A!=3,!B,B>=6,!C,C==6,!D,D!=5,F: 5
- 11 A,A!=6,!B,B>=6,C==2,D==0,G: 3
- 12 !A,A!=6,B==0,C,C<=6,D!=2,F: 5
- 13 !A,A<=7,B==6,C==0,D==4,F: 2
- 14 A<=4,!B,B!=4,C!=7,D>=0,G: 6

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## Activated Rules

Protein Rules:

- 4 !A,A<=2,B<=0,C,C!=6,D!=5,->B
- 6 !A,A<=4,!B,B!=4,C>=1,D<=0,->D
- 10 !A,A!=3,B!=1,!C,C<=7,D!=0,->C
- 13 A==0,B,B!=7,C!=1,D!=1,->C

Architecture Rules:

- 3 A!=1,B<=5,C<=3,!D,D>=0,F: 7
- 4 !A,A<=6,B!=4,C!=1,D<=5,G: 1
- 6 A==0,B!=6,!C,C!=7,D<=7,F: 0
- 8 !A,A<=4,!B,B!=3,C!=4,!D,D<=5,G: 7
- 9 A==0,B<=3,C,C<=1,D==0,F: 3
- 12 !A,A!=6,B<=0,C,C<=6,D!=2,F: 5
- 14 A<=4,!B,B!=4,C!=7,D>=0,G: 6

- 4 protein rules have formed a GRN
- Activate different architecture rules in different cells

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